

## Peruvian Computing Society (SPC)

School of Computer Science Sillabus 2021-I

### 1. COURSE

CS1D1. Discrete Structures I (Mandatory)

### 2. GENERAL INFORMATION

**2.1** Credits : 4

**2.2 Theory Hours** : 2 (Weekly)

2.3 Practice Hours : -

2.4 Duration of the period : 16 weeks
2.5 Type of course : Mandatory
2.6 Modality : Face to face

2.7 Prerrequisites : None

### 3. PROFESSORS

Meetings after coordination with the professor

### 4. INTRODUCTION TO THE COURSE

Discrete structures provide the theoretical foundations necessary for computation. These fundamentals are not only useful to develop computation from a theoretical point of view as it happens in the course of computational theory, but also is useful for the practice of computing; In particular in applications such as verification, cryptography, formal methods, etc.

### 5. GOALS

- Apply Properly concepts of finite mathematics (sets, relations, functions) to represent data of real problems.
- Model real situations described in natural language, using propositional logic and predicate logic.
- Determine the abstract properties of binary relations.
- Choose the most appropriate demonstration method to determine the veracity of a proposal and construct correct mathematical arguments.
- Interpret mathematical solutions to a problem and determine their reliability, advantages and disadvantages.
- Express the operation of a simple electronic circuit using Boolean algebra.

## 6. COMPETENCES

- a) An ability to apply knowledge of mathematics, science. (Usage)
- j) Apply the mathematical basis, principles of algorithms and the theory of Computer Science in the modeling and design of computational systems in such a way as to demonstrate understanding of the equilibrium points involved in the chosen option. (Usage)

### 7. SPECIFIC COMPETENCES

- **a1)** Apply demonstration techniques (direct method, contrapositive, induction and contradiction) to demonstrate properties in discrete structures and algorithms.
- **a2)** Use logical propositions in an orderly manner.
- **a3)** Apply counting techniques in solving computer problems.
- j1) Solve recurrence problems to simplify algorithmic complexity
- **j2)** Apply graph and tree theory for optimization and problem solving

# 8. TOPICS

Unit 1: Sets, Relations, and Functions (22)

Competences Expected: a,j

Topics	Learning Outcomes
<ul> <li>Sets         <ul> <li>Venn diagrams</li> <li>Union, intersection, complement</li> <li>Cartesian product</li> <li>Power sets</li> <li>Cardinality of finite sets</li> </ul> </li> <li>Relations:         <ul> <li>Reflexivity, simmetry, transitivity</li> <li>Equivalence relations</li> <li>Partial order relations and sets</li> <li>Extremal elements of a partially ordered sets</li> </ul> </li> <li>Functions         <ul> <li>Surjections, injections, bijections</li> <li>Inverses</li> <li>Composition</li> </ul> </li> </ul>	<ul> <li>Explain with examples the basic terminology of functions, relations, and sets [Assessment]</li> <li>Perform the operations associated with sets, functions, and relations [Assessment]</li> <li>Relate practical examples to the appropriate set, function, or relation model, and interpret the associated operations and terminology in context [Assessment]</li> </ul>
<b>Readings</b> : [Gri03], [Ros07], [Vel06]	

Unit 2: Basic Logic (14) Competences Expected: a,j		
<ul> <li>Propositional logic</li> <li>Logical connectives</li> <li>Truth tables</li> <li>Normal forms (conjunctive and disjunctive)</li> <li>Validity of well-formed formula</li> <li>Propositional inference rules (concepts of modus ponens and modus tollens)</li> <li>Predicate logic  – Universal and existential quantification</li> <li>Limitations of propositional and predicate logic (e.g., expressiveness issues)</li> </ul>	<ul> <li>Convert logical statements from informal language to propositional and predicate logic expressions [Usage]</li> <li>Apply formal methods of symbolic propositional and predicate logic, such as calculating validity of formulae and computing normal forms [Usage]</li> <li>Use the rules of inference to construct proofs in propositional and predicate logic [Usage]</li> <li>Describe how symbolic logic can be used to model real-life situations or applications, including those arising in computing contexts such as software analysis (eg, program correctness), database queries, and algorithms [Familiarity]</li> <li>Apply formal logic proofs and/or informal, but rigorous, logical reasoning to real problems, such as predicting the behavior of software or solving problems such as puzzles [Usage]</li> <li>Describe the strengths and limitations of propositional and predicate logic [Usage]</li> </ul>	
<b>Readings</b> : [Ros07], [Gri03], [Vel06]		
G [ ], [ ], [ ]		

Unit 3: Proof Techniques (14)		
Competences Expected: a,j		
Topics	Learning Outcomes	
<ul> <li>Notions of implication, equivalence, converse, inverse, contrapositive, negation, and contradiction</li> <li>The structure of mathematical proofs</li> <li>Direct proofs</li> <li>Disproving by counterexample</li> </ul>	<ul> <li>Identify the proof technique used in a given proof [Assessment]</li> <li>Outline the basic structure of each proof technique (direct proof, proof by contradiction, and induction) described in this unit [Usage]</li> <li>Apply each of the proof techniques (direct proof, proof by contradiction, and induction) correctly in the construction of a sound argument [Usage]</li> <li>Determine which type of proof is best for a given</li> </ul>	
<ul><li> Proof by contradiction</li><li> Induction over natural numbers</li></ul>		
<ul> <li>Structural induction</li> <li>Weak and strong induction (i.e., First and Second Principle of Induction)</li> <li>Recursive mathematical definitions</li> </ul>	<ul> <li>problem [Assessment]</li> <li>Explain the parallels between ideas of mathematical and/or structural induction to recursion and recursively defined structures [Familiarity]</li> </ul>	
• Well orderings	<ul> <li>Explain the relationship between weak and strong induction and give examples of the appropriate use of each [Assessment]</li> <li>State the well-ordering principle and its relationship to mathematical induction [Familiarity]</li> </ul>	
Readings: [Ros07], [Sch12], [Vel06]		

Unit 4: Data Representation (10)		
Competences Expected: a,j		
Topics	Learning Outcomes	
<ul> <li>Numerical representation: sign-magnitude, floating point.</li> <li>Representation of other objects: sets, relations, functions.</li> </ul>	<ul> <li>Explain numerical representations such as sign-magnitude and floating point. [Assessment].</li> <li>Carry out arithmetic operations using different kinds of representations. [Assessment].</li> <li>Explain the floating point standard IEEE-754 [Familiarity].</li> </ul>	
<b>Readings</b> : [Ros07], [Gri03], [Vel06]		

### 9. WORKPLAN

## 9.1 Methodology

Individual and team participation is encouraged to present their ideas, motivating them with additional points in the different stages of the course evaluation.

## 9.2 Theory Sessions

The theory sessions are held in master classes with activities including active learning and roleplay to allow students to internalize the concepts.

## 9.3 Practical Sessions

The practical sessions are held in class where a series of exercises and/or practical concepts are developed through problem solving, problem solving, specific exercises and/or in application contexts.

## 10. EVALUATION SYSTEM

\*\*\*\*\*\* EVALUATION MISSING \*\*\*\*\*\*

## 11. BASIC BIBLIOGRAPHY

- [Gri03] R. Grimaldi. Discrete and Combinatorial Mathematics: An Applied Introduction. 5 ed. Pearson, 2003.
- [Ros07] Kenneth H. Rosen. Discrete Mathematics and Its Applications. 7 ed. Mc Graw Hill, 2007.
- [Sch12] Edward R. Scheinerman. Mathematics: A Discrete Introduction. 3 ed. Brooks Cole, 2012.
- [Vel06] Daniel J. Velleman. How to Prove It: A Structured Approach. Ed. by Cambridge University Pres. 2nd. 2006. ISBN: 978-0521675994.